
TES-Simulations

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X-ray Integral Field Unit

X-IFU photon detection process:

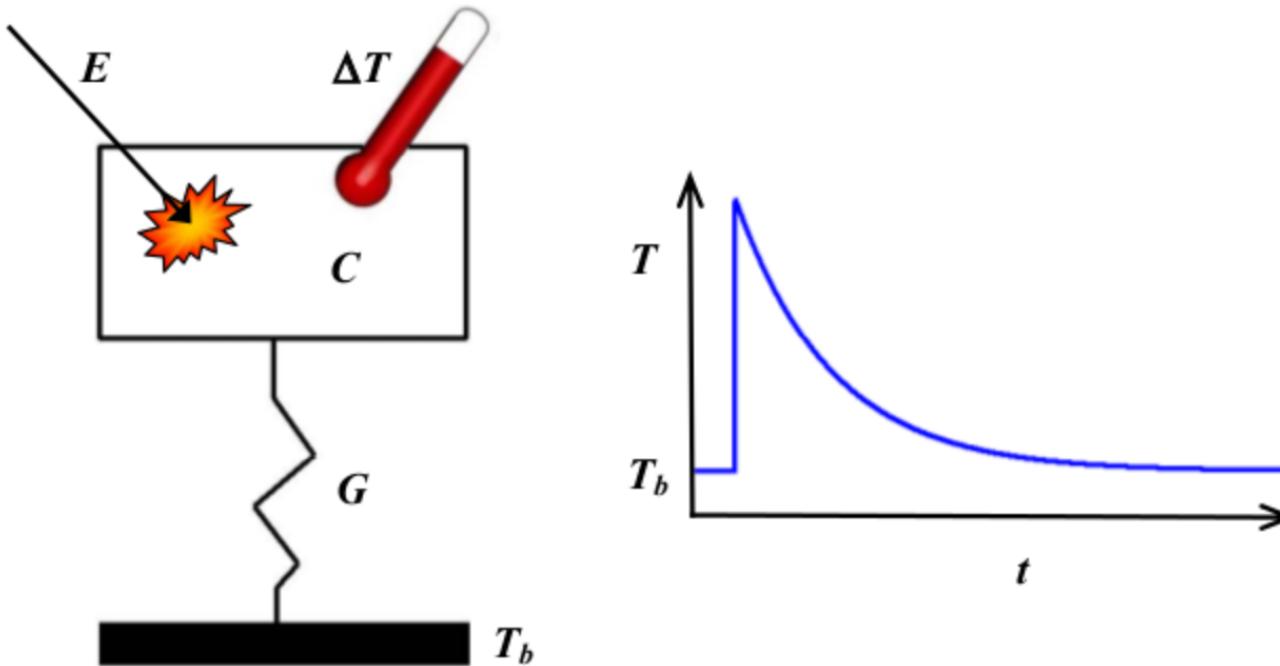
- sensitivity described by effective area curves
(taking into account mirror reflectivity, pixel sensitivity, gaps)
- Two (input/output-compatible) simulation approaches
 - **xifupipeline**:
 - * full imaging implemented
 - * fast detection simulation using response matrices

⇒ Well suited for faint sources
 - **tessim/sirena**
 - * Simulation of TES physics and pulse reconstruction
 - * Slower than xifupipeline, but much better physics

⇒ Well suited for bright sources

⇒ Well suited for engineering studies

Device Simulations: Principle



Smith (2006 PhD Leicester)

Calorimeter: measure temperature change in device with temperature T_0 connected to heat bath with temperature T_S .

Joule heating by current through device $\Rightarrow T_0 > T_S$

Absorption: temperature rises: $\Delta T = E_\gamma/C$

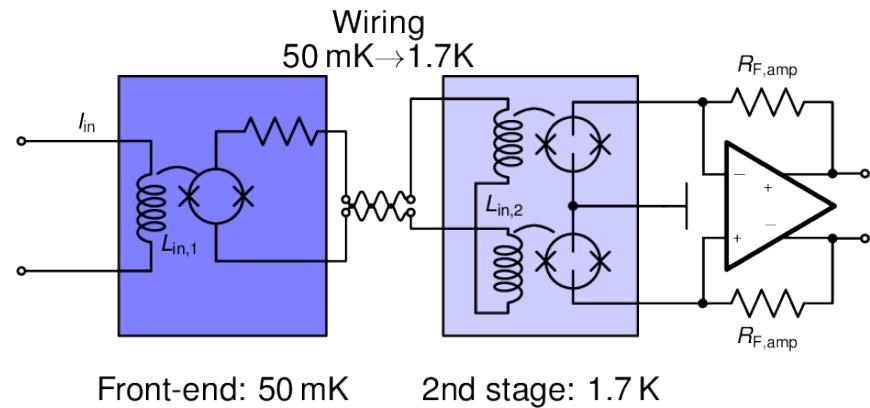
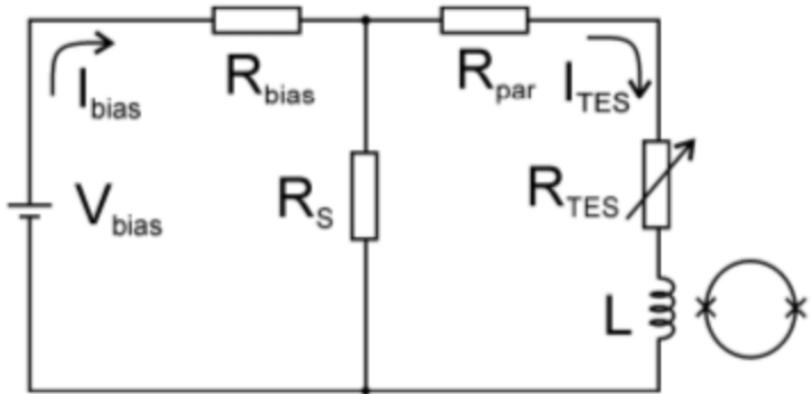
C : heat capacity

Relaxes back to T_0 . Typical timescale: $\tau = C/G$.

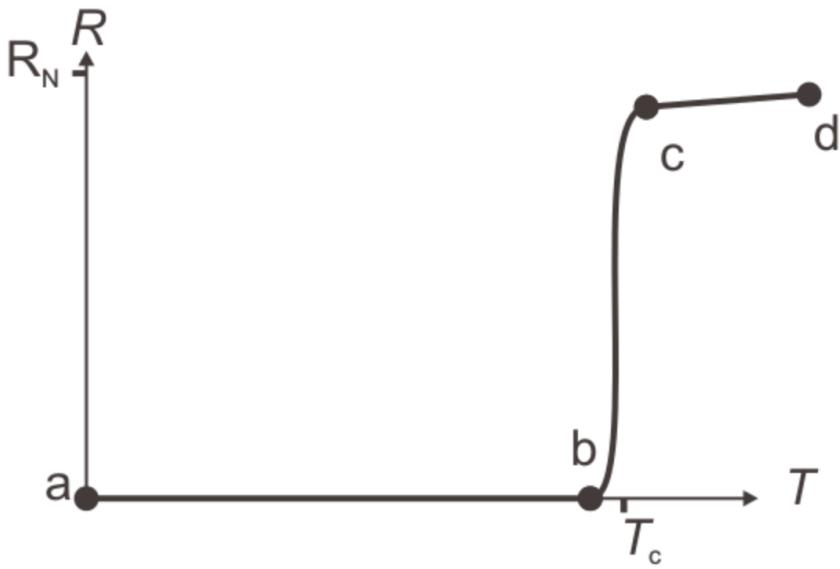
Resolution given by thermal fluctuations: $\Delta E = 2.35\sqrt{kT^2C}$

\Rightarrow Small (**few eV**) for T small (mK)

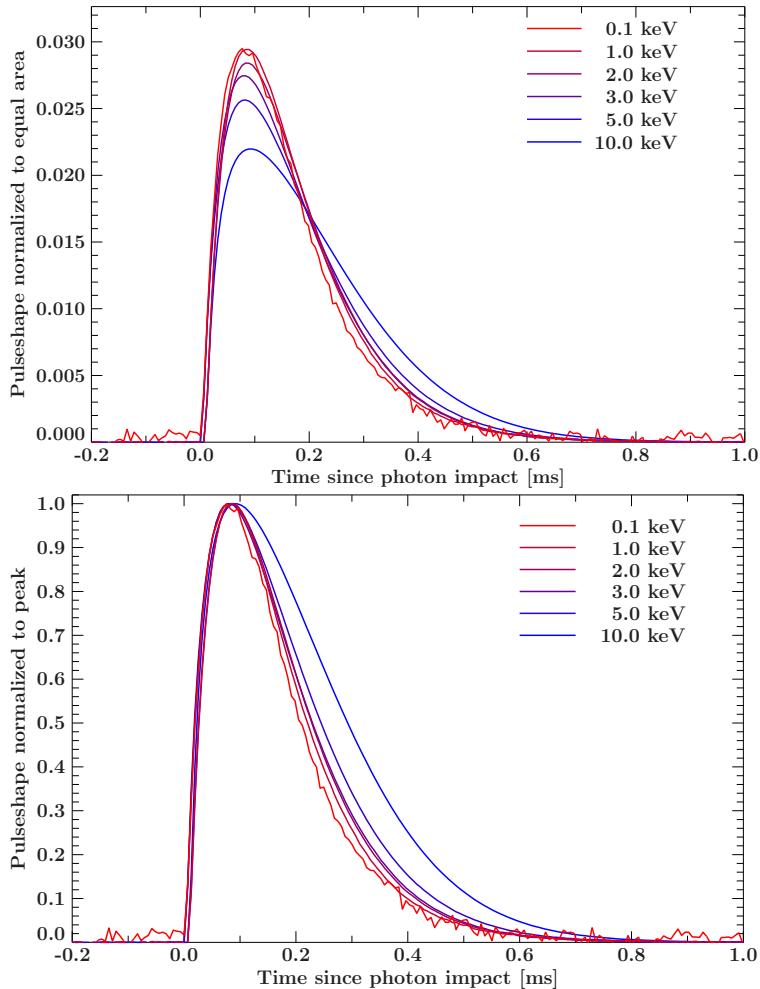
Device Simulations: Principle



Kinnunen (2011, PhD Jyväskylä)



negative electrothermal feedback: Operate circuit at **Transition Edge** between superconduction and normal conduction, **voltage bias** circuit:
 absorption $\Rightarrow R \nearrow$
 \Rightarrow Joule power $P_J = I^2 R \searrow$
 \Rightarrow faster cooling than for $R = \text{const}$
 Typical time constants 75 $\mu\text{s} \dots 400 \mu\text{s}$



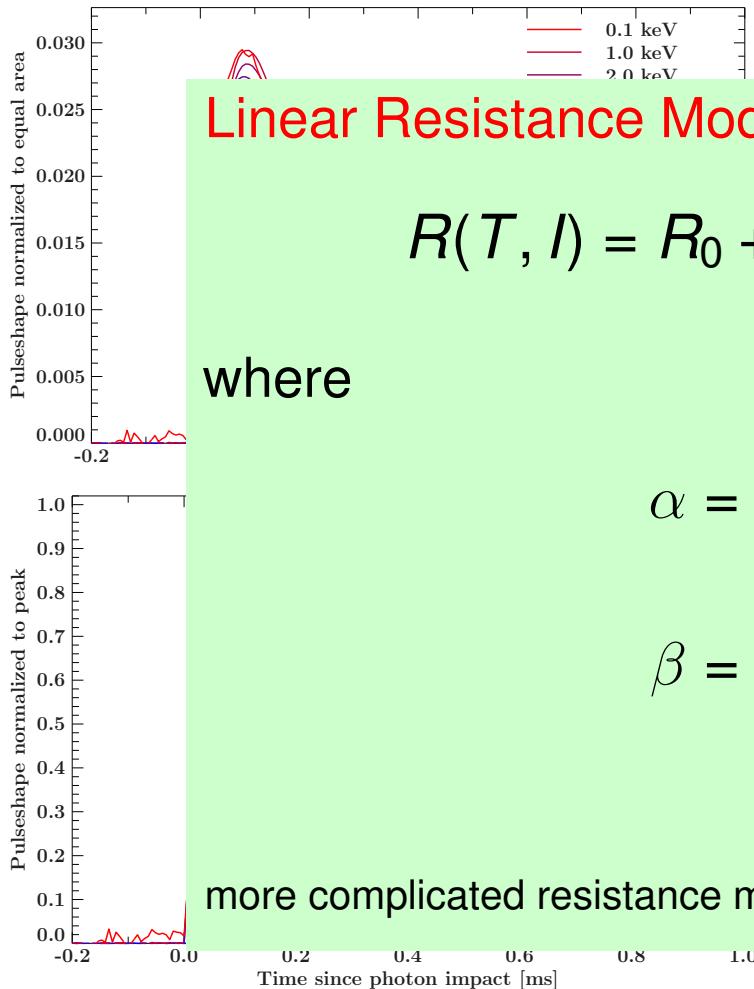
Typical pulse shapes for 0.1, 1, 2, 3, 5, 10 keV, normalized to top: equal area, bottom: peak current.

- based on GSFC code by S.J. Smith
- numerical solution of differential equations for $T(t)$, $I(t)$ (e.g., Irwin & Hilton, 2005),

$$C \frac{dT}{dt} = -P_b + P_J + P + \text{Noise}$$

$$L \frac{dI}{dt} = V - IR_L - IR(T, I) + \text{Noise}$$

- linear resistance model, $R(T, I; \alpha, \beta)$
- noise treatment: Johnson of circuit, bath, excess noise
- input parameters: C , G_b , n , α , β , m , R_0 , T_0 , T_b , L_{crit}
including flexible, FITS-based library of pixel types



Linear Resistance Model:

$$R(T, I) = R_0 + \frac{\partial R}{\partial T} \Big|_{I_0} (T - T_0) + \frac{\partial R}{\partial I} \Big|_{T_0} (I - I_0) \quad (1)$$

where

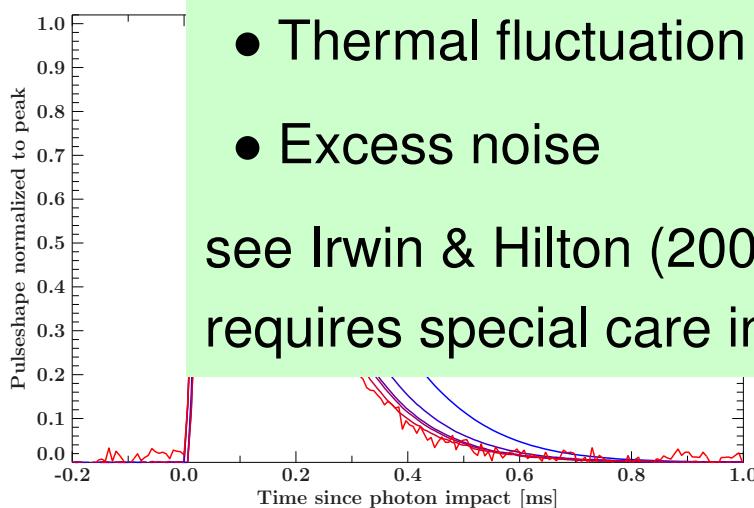
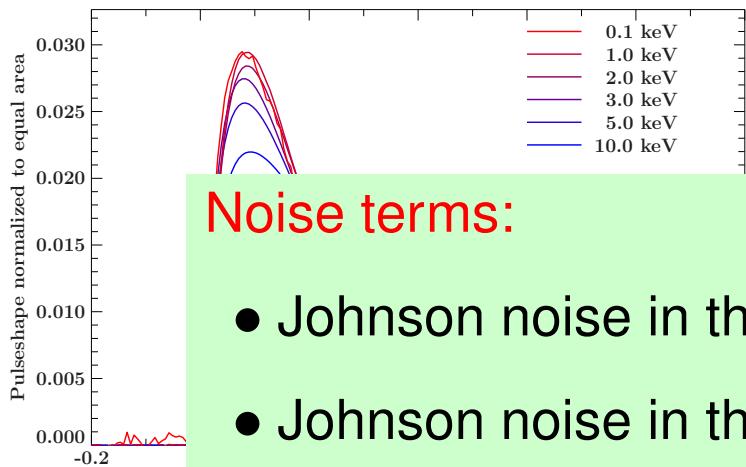
$$\alpha = \frac{\partial \log R}{\partial \log T} \Big|_{I_0} = \frac{T_0}{R_0} \frac{\partial R}{\partial T} \Big|_{I_0} \quad (2)$$

$$\beta = \frac{\partial \log R}{\partial \log I} \Big|_{T_0} = \frac{I_0}{R_0} \frac{\partial R}{\partial I} \Big|_{T_0} \quad (3)$$

more complicated resistance models also exist ("cross talk")

Typical pulse shapes for 0.1, 1, 2, 3, 5, 10 keV, normalized to top: equal area, bottom: peak current.

- input parameters: C , G_b , n , α , β , m , R_0 , T_0 , T_b , L_{crit}
including flexible, FITS-based library of pixel types



Typical pulse shapes for 0.1, 1, 2, 3, 5, 10 keV, normalized to top: equal area, bottom: peak current.

- based on GSFC code by S.J. Smith

Noise terms:

- Johnson noise in the TES
- Johnson noise in the load resistor
- Thermal fluctuation noise
- Excess noise

see Irwin & Hilton (2005) for details

requires special care in numerical integrator

- **NOISE TREATMENT.** comparison of circuit, bath, excess noise
- input parameters: C , G_b , n , α , β , m , R_0 , T_0 , T_b , L_{crit}
including flexible, FITS-based library of pixel types

Parameter	IXO baseline	DM	LPA	SPA
Pixel size	249 μm	249 μm	249 - 300 μm	75 - 110 μm
Heat capacity, C @ T_0	0.8 pJ/K	0.8 pJ/K	0.8 pJ/K	0.26 pJ/K
Bath conductance, G_b @ T_0	200 pW/K	115 pW/K	57 pW/K	300 pW/K
Temperature exponent, n	3.0	3.0	3.0	4.0
α	75	75	75	100
β	1.25	1.25	1.25	10
Unexplained noise factor, M	0	0	0	0.8
Resistance, R_0	1 m Ω	1 m Ω	1 m Ω	1.1 m Ω
Current, I_0	69.5 μA	52.5 μA	37.1 μA	73.5 μA
Temperature, T_0	90 mK	90 mK	90 mK	90 mK
Power, P_0	4.81 pW	2.76 pW	1.38 pW	5.95 pW
R_{shunt}^*	49 $\mu\Omega$	90 $\mu\Omega$	207 $\mu\Omega$	91 $\mu\Omega$
Transformer Turns Ratio *	5.53	4.08	2.69	4.05
L_{crit}	66 nH	120 nH	276 nH	122 nH
τ_{eff}	431 μs	0.795 ms	1.87 ms	305 μs
τ_{crit}	156 μs	286 μs	649 μs	78 μs
Time constraint for 80% high res.	8.6 ms	112 ms	112 ms	4 ms
ΔE_{FWHM} (∞ rec length, small signal)	1.69 eV	1.70 eV	1.73 eV	1.54 eV
ΔE_{FWHM} (high res, small signal)	1.83 eV	1.71 eV	1.76 eV	1.69 eV
Max slew rate / keV	88 mA/s/keV	36 mA/s/keV	11 mA/s/keV	229 mA/s/keV
f_{eff} - effective / information bandwidth	970 Hz	560 Hz	280 Hz	1710 Hz

Source: Steve Smith, GSFC, 29-05-2015

* Assumes 1.5 m Ω parasitic from capacitive element, and filter L = 2 μH , $T_{\text{shunt}} = 70\text{mK}$

Parameter	IXO baseline	DM	LPA	SPA
Pixel size	249 μm	249 μm	249 - 300 μm	75 - 110 μm
Heat capacity, C @ T_0	0.8 pJ/K	0.8 pJ/K	0.8 pJ/K	0.26 pJ/K
Bath conductance, G_b @ T_0	200 pW/K	115 pW/K	57 pW/K	300 pW/K
Temperature exponent, n	3.0	3.0	3.0	4.0
α	75	75	75	100
β	1.25	1.25	1.25	10
Unexplained noise factor, M	0	0	0	0.8
Resistance, R_0	1 m Ω	1 m Ω	1 m Ω	1.1 m Ω
Current, I_0	62.5 μA	50.5 μA	37.1 μA	73.5 μA
Temperature, T_0			90 mK	90 mK
Power, P_0			1.38 pW	5.95 pW
R_{shunt}^*			207 $\mu\Omega$	91 $\mu\Omega$
Transformer Turns Ratio *			2.69	4.05
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Note: Parameters are outdated!

Source: Steve Smith, GSFC, 29-05-2015

* Assumes 1.5 m Ω parasitic from capacitive element, and filter L = 2 μH , $T_{\text{shunt}} = 70\text{mK}$

Translation to program: (too) many parameters ;-)

```

Parameters for /home/wilms/pfiles/tessim.par
  PixType = SPA           Pixel type
  PixID = 1                Number of pixel
  PixImpList = test_slow.fits File name of pixel impact list
  Streamfile = stream.fits File name of output FITS stream
    (tstart = 0.)          Start time of simulation [s]
    (tstop = 1.)           Stop time of simulation [s]
  (sample_rate = 156.25e3) Sample rate [Hz]
    (acbias = y)          AC biased (yes) or DC biased (no)
    (T_start = 90.0)       Initial operating temperature [mK]
    (Ce = 0.26)           Heat capacity [pJ/K]
    (Gb = 300)            Bath conductance [pW/K]
    (n = 4.0)              Temperature exponent
    (alpha = 100.)         TES sensitivity alpha (T/R*dR/dT)
    (beta = 10.)           TES current dependence beta (I/R*dR/dI)
  (m_excess = 0.8)        Magnitude of unexplained (excess) noise
    (R0 = 1.1)             Operating point resistance R0 [mOhm]
    (I0 = 72.5)            Current [muA]
    (Tb = 55)              Heat sink/bath temperature Tb [mK]
    (RL = 0.0)             Shunt/load resistor value RL [mOhm]
  (Rparasitic = 0.)       Parasitic resistor value Rparasitic [mOhm]
    (TTR = 4.11)           Transformer Turns Ratio
    (Lin = 238.)           Circuit inductance [nH]
    (Lfilter = 2.)          Filter inductance [muH]
    (V0 = -1.)              Effective voltage bias [muV]
  (thermalBias = n)       Calculate I0 and V0 from thermal power balance?
    (Pload = 0.0)           Residual optical load power [pW]
    (bias = 15)             Bias percentage of normal resistance in the transition
    (imin = -1e-8)          TES current corresponding to 0 ADU [A]
    (imax = 5e-5)           TES current corresponding to 65534 ADU [A]
    (simnoise = y)          Simulate noise?
      Use the stochastic integrator? (default no)
  (stochastic_integrator = n) Option to use the 2 fluid model of RTI transition (default no)
    (twofluid = n)          Option to use frame hits (default no). Requires time of event and file name
    (frame_hit = n)         Time of frame event (s)
  (frame_hit_time = 0.)     File name of frame hit model
  (frame_hit_file = none)  Trigger type
    (triggertype = stream) Size of a trigger
    (triggersize = 1024)    Size of the prebuffer
    (prebuffer = 128)       Display properties of TES and exit without calculation?
  (propertiesonly = n)      Seed for the noise RNG (0 to use system time)
    (Seed = 0)               Display progress bar?
  (progressbar = y)         Overwrite output files?
    (clobber = y)            Simulate Crosstalk (yes/no)?
  (doCrosstalk = y)         Readout mode for output current ['total': Absolute value, 'I': I-channel, 'Q':Q-channel]
  (readoutMode = total)

```

Configuration control

Solution to large number of parameter problem:

self documentation \Rightarrow store all parameters in FITS files output by tessim: can reload exact pixel configuration from any stream produced by tessim:

First run tessim with propertiesonly=yes:

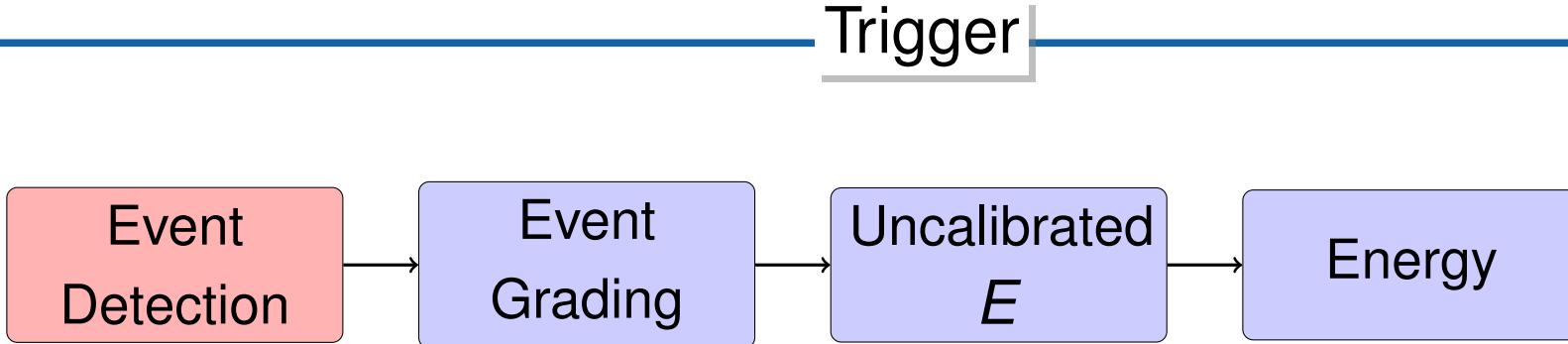
```
tessim PixType=LPA Ce=0.26 Gb=280 ... propertiesonly=yes  
... Streamfile=testpixel.fits
```

Later run with

```
tessim PixType=file:testpixel.fits[LPA]  
Streamfile=simulation PixImpList=impact.fits
```

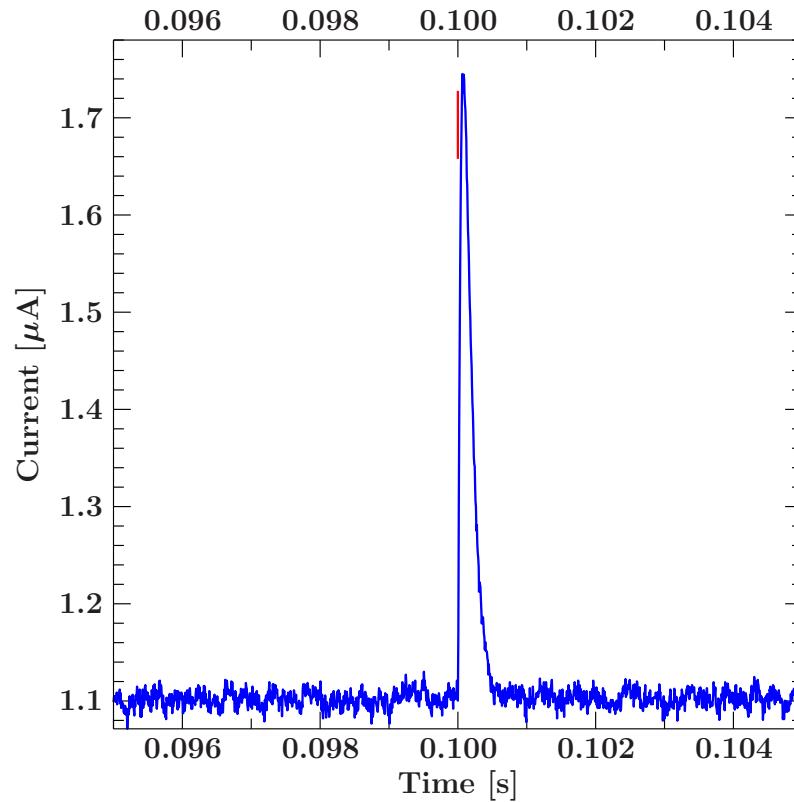
where ... [LPA] : FITS selection syntax on FITS HDUNAME keyword.
impact.fits

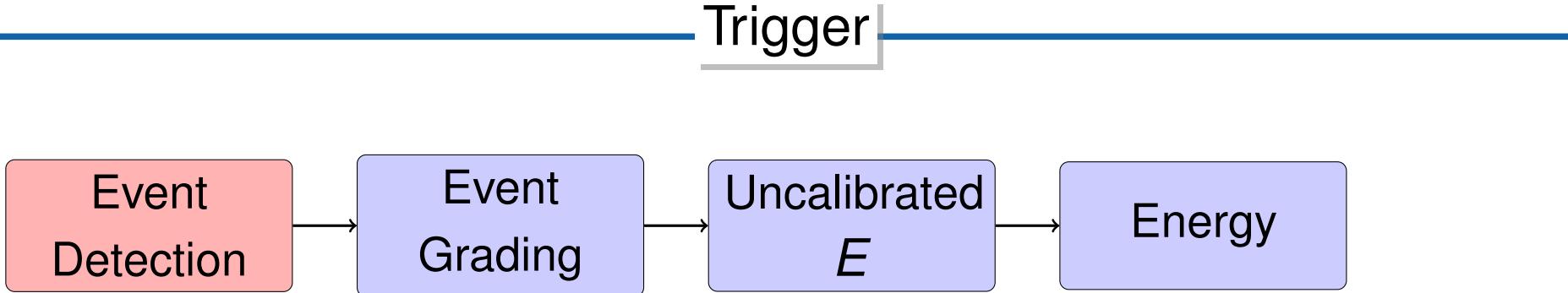
: FITS impact file with TIME and ENERGY columns.



Iterative Event Detection (Triggering):

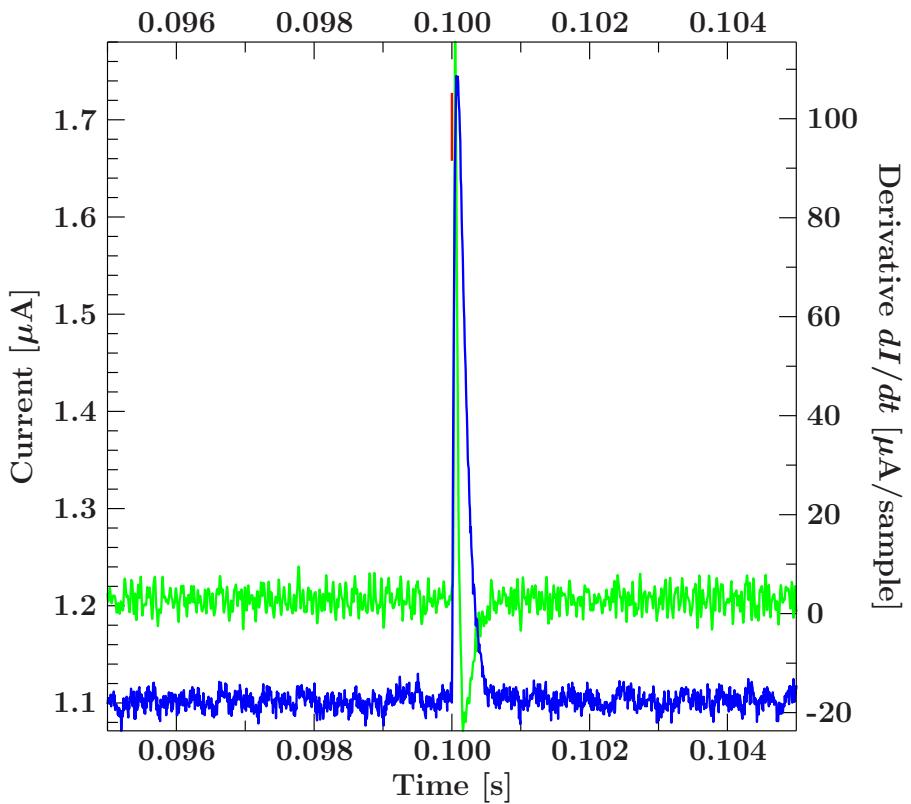
- Take derivative of TES stream
- trigger=
- stream
 - movavg:npts:threshold:suppress
 - diff:npts:threshold:suppress
- remove pulses on the go to find others

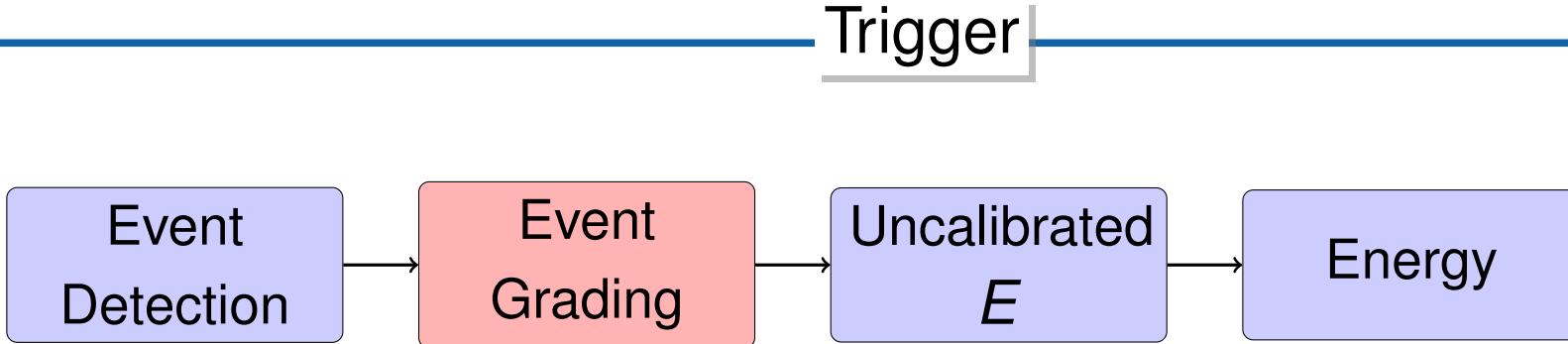




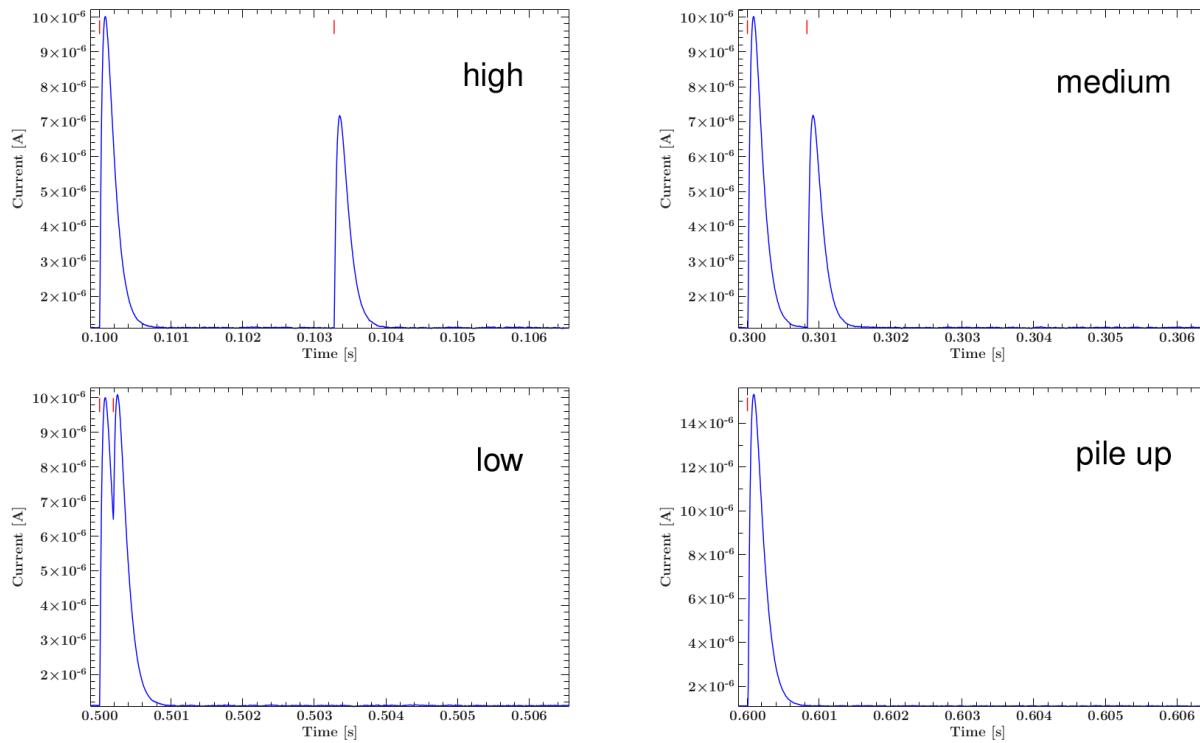
Iterative Event Detection (Triggering):

- Take derivative of TES stream
`trigger=`
 – stream
 – movavg:npts:threshold:suppress
 – diff:npts:threshold:suppress
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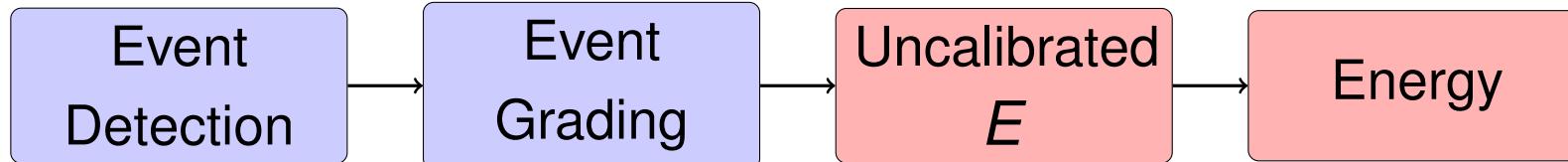




Event Grading: Resolution depends on distance between different pulses.



Trigger



Energy calculation: Use optimal filter
(Szymkowiak et al., 1993):

$$E \propto \sum \frac{D(f)S^*(f)}{N(f)}$$

where

- $D(f)$: data spectrum,
- $S(f)$: template spectrum,
- $N(f)$: noise spectrum

Caveats:

- exact degradation at higher energies not yet studied for time reasons
- reconstruction algorithms still in development and under optimization, have done first studies using principle component analysis and resistance space optimal filtering